

## Math 4A Week 10 – December 8, 2014

1. An elementary row operation on  $A$  does not change the determinant. True or false?
2. Matrix  $A$  has eigenvalue  $\lambda = 2$  and eigenvector  $x = (3, 1)$ . Find  $A^{10}x$ .
3. Let  $\lambda$  be an eigenvalue of an invertible matrix  $A$ . What is the eigenvalue of  $A^{-1}$ ?
4. Are two diagonal matrices always similar?
5. Prove: If  $A$  and  $B$  are similar, they have the same characteristic polynomial.
6.  $A$  is an  $n \times n$  matrix. True or False:
  - (i). If  $\mathbb{R}^n$  has a basis of eigenvectors of  $A$ , then  $A$  is diagonalizable.
  - (ii). If  $A$  is diagonalizable, then  $A$  is invertible.
  - (iii).  $A$  is diagonalizable if  $A$  has  $n$  eigenvectors.
  - (iv). If  $A$  is diagonalizable, then  $A$  has  $n$  distinct eigenvalues.
7. Diagonalize the following matrix if possible:

$$A = \begin{bmatrix} 5 & 0 & 0 & 0 \\ 0 & 5 & 0 & 0 \\ 1 & 4 & -3 & 0 \\ -1 & -2 & 0 & -3 \end{bmatrix}$$

Solution: See Section 5.3 Example 6.